

Please write clearly in block capitals.		
Centre number	Candidate number	
Surname		
Forename(s)		
Candidate signature		

AS **MATHEMATICS**

Unit Further Pure 1

Wednesday 15 June 2016 Morning Time allowed: 1 hour 30 minutes

Materials

For this paper you must have:

• the blue AQA booklet of formulae and statistical tables.

You may use a graphics calculator.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer all questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do not use the space provided for a different question.
- Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.



Answer all questions.

Answer each question in the space provided for that question.

- **1** The quadratic equation $x^2 6x + 14 = 0$ has roots α and β .
 - (a) Write down the value of $\alpha + \beta$ and the value of $\alpha\beta$.

[2 marks]

(b) Find a quadratic equation, with integer coefficients, which has roots $\frac{\alpha}{\beta}$ and $\frac{\beta}{\alpha}$.

[5 marks]

QUESTION PART REFERENCE	Answer space for question 1



QUESTION PART REFERENCE	Answer space for question 1
THE ENERGE	



2 A curve C has equation $\underline{\cdot}$	y = (2 - x)(1 + x) + 3.
---	-------------------------

(a) A line passes through the point (2, 3) and the point on C with x-coordinate 2 + h. Find the gradient of the line, giving your answer in its simplest form.

[3 marks]

(b) Show how your answer to part (a) can be used to find the gradient of the curve C at the point (2, 3). State the value of this gradient.

[2 marks]

QUESTION PART REFERENCE	Answer space for question 2
REFERENCE	



QUESTION PART REFERENCE	Answer space for question 2
REFERENCE	



3 The variables y and x are related by an equation of the form

$$y = a(b^x)$$

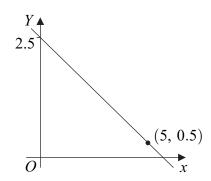
where a and b are positive constants.

Let
$$Y = \log_{10} y$$
.

(a) Show that there is a linear relationship between Y and x.

[2 marks]

(b) The graph of Y against x, shown below, passes through the points (0, 2.5) and (5, 0.5).



(i) Find the gradient of the line.

[1 mark]

(ii) Find the value of a and the value of b, giving each answer to three significant figures. [4 marks]

QUESTION	Anower anges for guestian 2
QUESTION PART REFERENCE	Answer space for question 3
THE ENERGE	

QUESTION PART REFERENCE	Answer space for question 3
REFERENCE	



4 (a) Given that $\sin \frac{\pi}{3} = \cos \frac{\pi}{k}$, state the value of the integer k.

[1 mark]

(b) Hence, or otherwise, find the general solution of the equation

$$\cos\left(2x - \frac{5\pi}{6}\right) = \sin\frac{\pi}{3}$$

giving your answer, in its simplest form, in terms of π .

[4 marks]

(c) Hence, given that $\cos\left(2x - \frac{5\pi}{6}\right) = \sin\frac{\pi}{3}$, show that there is only one finite value for $\tan x$ and state its exact value.

[2 marks]

QUESTION PART REFERENCE	Answer space for question 4
PAR I REFERENCE	Answer space for question 4



QUESTION PART REFERENCE	Answer space for question 4
KEFERENCE	



5 (a)	Use the formulae for			$\sum_{n=0}^{\infty} (6r - 3)^2 = 3n(4n^2)$	- 1).
		r=1	r=1	r=1	[5 marks]

(b) Hence express $\sum_{r=1}^{2n} r^3 - \sum_{r=1}^{n} (6r-3)^2$ as a product of four linear factors in terms of n. [4 marks]

OUESTION	
QUESTION PART REFERENCE	Answer space for question 5



QUESTION PART REFERENCE	Answer space for question 5
THE ENERGE	



6	A parabola with equation $y^2=4ax$, where a is a constant, is translated by the	
	vector $\begin{bmatrix} 2 \\ 3 \end{bmatrix}$ to give the curve C . The curve C passes through the point $(4, 7)$.	
(a		
	[3	marks]
(b	Find the values of k for which the line $ky=x$ does not meet the curve C . [6]	marks]
QUESTION PART	Answer space for question 6	
REFERENCE	E .	



QUESTION PART REFERENCE	Answer space for question 6
THE ENERGE	



7 (a) Solve the equation $x^2 + 4x + 20 = 0$, giving your answers in the form c + di, where c and d are integers.

[3 marks]

(b) The roots of the quadratic equation

$$z^2 + (4 + i + qi)z + 20 = 0$$

are w and w^* .

(i) In the case where q is real, explain why q must be -1 .

[2 marks]

(ii) In the case where w = p + 2i, where p is real, find the possible values of q.

[5 marks]

OUESTION	
QUESTION PART REFERENCE	Answer space for question 7
REFERENCE	



QUESTION PART REFERENCE	Answer space for question 7
NEI ENENGE	



QUESTION PART REFERENCE	Answer space for question 7



QUESTION PART REFERENCE	Answer space for question 7
REFERENCE	



8 The matrix **A** is defined by $\mathbf{A} = \begin{bmatrix} 2 & 0 \\ 0 & 1 \end{bmatrix}$.

(a) (i) Find the matrix A^2 .

[1 mark]

- (ii) Describe fully the single geometrical transformation represented by the matrix ${\bf A}^2$. [1 mark]
- (b) Given that the matrix **B** represents a reflection in the line $x + \sqrt{3}y = 0$, find the matrix **B**, giving the exact values of any trigonometric expressions.

[2 marks]

Hence find the coordinates of the point P which is mapped onto (0, -4) under the transformation represented by \mathbf{A}^2 followed by a reflection in the line $x + \sqrt{3}y = 0$.

[6 marks]

QUESTION PART REFERENCE	Answer space for question 8



QUESTION PART REFERENCE	Answer space for question 8
NEI ERENGE	



QUESTION PART REFERENCE	Answer space for question 8
NEI ENEIVOE	



QUESTION PART REFERENCE	Answer space for question 8
NEI ERENGE	



9 A curve *C* has equation $y = \frac{x-1}{(x-2)(2x-1)}$.

The line L has equation $y = \frac{1}{2}(x-1)$.

(a) Write down the equations of the asymptotes of C.

[2 marks]

(b) By forming and solving a suitable cubic equation, find the x-coordinates of the points of intersection of L and C.

[3 marks]

(c) Given that C has no stationary points, sketch C and L on the same axes.

[3 marks]

(d) Hence solve the inequality $\frac{x-1}{(x-2)(2x-1)} \ge \frac{1}{2}(x-1)$.

[3 marks]

QUESTION PART REFERENCE	Answer space for question 9
TE ETETOE	



QUESTION PART REFERENCE	Answer space for question 9
NEI ENENGE	



QUESTION PART REFERENCE	Answer space for question 9

END OF QUESTIONS

Copyright information

For confidentiality purposes, from the November 2015 examination series, acknowledgements of third party copyright material will be published in a separate booklet rather than including them on the examination paper or support materials. This booklet is published after each examination series and is available for free download from www.aqa.org.uk after the live examination series.

Permission to reproduce all copyright material has been applied for. In some cases, efforts to contact copyright-holders may have been unsuccessful and AQA will be happy to rectify any omissions of acknowledgements. If you have any queries please contact the Copyright Team, AQA, Stag Hill House, Guildford, GU2 7XJ.

Copyright \circledcirc 2016 AQA and its licensors. All rights reserved.

